# Assessing treatment effect using registry data 

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## Motivation

Objective: decide whether a treatment is beneficial
$\rightarrow$ for a give time horizon
Material: registry data

- observational data (i.e. non-randomized)
- long term follow-up
- large number of patients

What do we mean by beneficial:

- does the treatment reduce the 1-year risk of developing the disease?


## Plan

(1) Estimating a 1-year risk of a disease using registry data
(2) Estimating a treatment effect using registry data
e.g. Staerk et al. 2016:

Stroke/thromboembolism


## Plan

(1) Estimating a 1-year risk of a disease using registry data $\rightarrow$ model checking [Cox]
(2) Estimating a treatment effect using registry data $\rightarrow$ model checking [new strategy]
e.g. Staerk et al. 2016:

Stroke/thromboembolism


## Absolute risk

## Definition

## 1-year absolute risk:

- chance that a person will be diagnosed with the event in 1 year
$\rightarrow$ depends on the risk of the event $\lambda_{\text {event }}$ $\rightarrow$ depends on the risk of death $\lambda_{\text {death }}$

Considering registry data, are involved: - the cuent of interest

- competing risks, e.g. death $\rightarrow$ mill nrevent the ohservation of the event


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covariates like age, gender
Considering registry data, are involved:
- the event of interest
- competing risks, e.g. death
$\rightarrow$ will prevent the observation of the event


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X: covariates like age, gender
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$$
r_{\text {event }}(t \mid X)=\underbrace{\int_{0}^{t}}_{\text {addition over time }} \underbrace{\substack{\text { ime event at time } s}}_{\text {survival at to time simmediate risk of }} \underbrace{\lambda_{\text {ever }}}_{\begin{array}{c}
\text { the } \\
S_{0}(s \mid X)
\end{array} \underbrace{}_{\text {event }}(s \mid X)} d s
$$

$X$ : covariates like age, gender ...
Considering registry data, are involved:

- the event of interest
- competing risks, e.g. death
$\rightarrow$ will prevent the observation of the event


## Cause specific Cox model

One Cox regression for each competing risk:

$$
\begin{aligned}
& \lambda_{\text {event }}(t \mid X)=\lambda_{0, \text { event }}(t) \exp \left(X \beta_{\text {event }}\right) \\
& \lambda_{\text {death }}(t \mid X)=\lambda_{0, \text { death }}(t) \exp \left(X \beta_{\text {death }}\right)
\end{aligned}
$$

## Cause specific Cox model

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& \lambda_{\text {death }}(t \mid X)=\lambda_{0, \text { death }}(t) \exp \left(X \beta_{\text {death }}\right)
\end{aligned}
$$

We can then estimate the overall survival.

- no event
- not dead


## Cause specific Cox model

One Cox regression for each competing risk:

$$
\begin{aligned}
& \lambda_{\text {event }}(t \mid X)=\lambda_{0, \text { event }}(t) \exp \left(X \beta_{\text {event }}\right) \\
& \lambda_{\text {death }}(t \mid X)=\lambda_{0, \text { death }}(t) \exp \left(X \beta_{\text {death }}\right)
\end{aligned}
$$

We can then estimate the overall survival.

$$
S_{0}(t \mid X)=\exp \left(-\int_{0}^{t} \lambda_{\text {death }}(s \mid X)+\lambda_{\text {event }}(s \mid X) d s\right)
$$

## In $\mathbb{R}$

1 > library(riskRegression)
$2>\operatorname{data}(M e l a n o m a)$
3 > fit1 <- CSC(formula=Hist(time,status)~sex+invasion+age,
4 + data=Melanoma)
5 fit1\$models\$`Cause 1`
Call:
survival:: coxph(...)

|  | coef | $\exp ($ coef $)$ | se(coef) | $z$ | $p$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| sexMale | 0.66338 | 1.94135 | 0.26632 | 2.49 | 0.01274 |
| invasionlevel.1 | 1.03717 | 2.82122 | 0.32824 | 3.16 | 0.00158 |
| invasionlevel.2 | 1.40323 | 4.06830 | 0.38074 | 3.69 | 0.00023 |
| age | 0.00982 | 1.00987 | 0.00834 | 1.18 | 0.23884 |

## $\ln \mathbb{R}$

1 > head(Melanoma[1:2,c("sex","invasion","age")])
sex invasion age
1 Male level. 176
2 Male level. 056
1 > predictRisk(fit1, newdata = Melanoma[1:2,],
2

$$
\text { cause }=1 \text {, time }=365.25 \text { ) }
$$

$$
365.25
$$

[1,] 0.06441670
[2,] 0.01992289

## Summary

We can easily compute the absolute risk

- using one Cox model for the event of interest
- using another Cox model for the competing events

But now we have to check the assumptions for each Cox model !

## Cox model assumptions

Assumptions:
(1) proportional hazard (PH) assumption
(2) (linear) functional form
(3) (absence of) interaction
[Not covered] non-informative censoring, influential observations

## Checking Cox model assumptions

Model checking is more complex compared to a linear regression

- several types of residuals
- many different diagnostic tools
- validity of the null hypothesis
e.g. PH vs. non PH
- against a specific alternative hypothesis
e.g. quadratic vs. linear effect age


## (1) Checking Proportional hazard assumption

Cox model:

$$
\lambda(t \mid X)=\lambda_{0}(t) e^{\beta X}
$$

Here we assume $\beta \Perp t$

- Visual checking with Kaplan Meier



## (1) Checking Proportional hazard assumption

Cox model:

$$
\lambda(t \mid X)=\lambda_{0}(t) e^{\beta X}
$$

Here we assume $\beta \Perp t$

- Statistical test: $\left(\mathcal{H}_{0}\right)$ the PH assumption holds, i.e. the cumulative score process follows a brownian bridge > plot(gof:: :cumres(coxph))

(1) Remedies for non proportional hazard Strategy 1: find the problematic variable and the type of time dependency
- Display of the Schoenfeld residuals (Grambsch et al. 1994)

$$
\mathbb{E}\left[r_{i j}\right] \approx \beta_{j}\left(t_{i}\right)-\hat{\beta}_{j}
$$


(1) Remedies for non proportional hazard Strategy 1: find the problematic variable and the type of time dependency

- Use a Cox model with time varying effects

$$
\lambda(t \mid X)=\lambda_{0}(t) e^{\beta(t) X}
$$

z1

> plot(timereg::timecox (Surv(time,status) $\sim$ z,

## (1) Remedies for non proportional hazard

Strategy 1: find the problematic variable and the type of time dependency

Strategy 2: stratification
Cox model:

$$
\lambda(t \mid X, \text { treatment })=\lambda_{0}(t) e^{\beta X+\gamma \text { treatment }}
$$

Stratified Cox model:

$$
\lambda(t \mid X, \text { treatment })=\lambda_{0, \text { treatment }}(t) e^{\beta X}
$$

## (2) Checking the functional form

$$
\lambda(t \mid X, T)=\lambda_{0} e^{\beta X}
$$

Here we assume the log of the risk increase linearly with $X$, e.g. with age.

Diagnostic tools:

- Display martingale residuals
- Comparison with model including a quadratic term or spline



## (3) Checking possible interactions

$$
\lambda(t \mid X, T)=\lambda_{0} e^{\beta X+\gamma t r e a t m e n t}
$$

Here we assume that the risk increase independently with $X$ and with treatment

Diagnostic tools:

- Display martingale residuals
- Comparison with a model with interactions



## Limits

In practice model validation is tedious:

- large number of tests
- at least 2 per variables + PH
(i.e. linearity and interaction with treatment)
- competing risks: two Cox models to check
- unclear alternative hypothesis
- residual plot can be hard to interpret
- large $n$ small $p$
- overpowered tests (Grøn et al. 2016)
$\rightarrow$ may detect unimportant deviations to hypothesis


## Average treatment effect

## Observational vs. randomized study

Randomized experiment

- eliminates confounding
- balances all risk factors: known AND unknown
$\rightarrow$ causal interpretation

Observational studies

- can ONLY account for known and measured risk factors
$\rightarrow$ establish associations

Causal inference theory:

- causal interpretation (under hypothesis) in observational studies


## Counterfactual outcomes

$\mathcal{H y p o t h e t i c a l}$ world


## Counterfactual outcomes

## Hypothetical world

We can measure for individual $i$ at time $t$ : $Y_{i}^{T=1}(t)$, outcome using intervention 1 $Y_{i}^{T=0}(t)$, outcome using intervention 0

We can estimate

$$
Y_{i}^{T=1}(t)-Y_{i}^{T=0}(t)
$$

the individual causal effect at $t$


## Counterfactual outcomes

Real world



## Counterfactual outcomes

Real world

We only can measure :

$$
Y_{i}^{T=1}(t) \quad \mathrm{OR} \quad Y_{i}^{T=0}(t)
$$



We can infer the average causal effect:

$$
\begin{aligned}
\operatorname{ACE}(t)= & \mathbb{E}\left[Y^{T=1}(t)-Y^{T=0}(t)\right] \\
= & \mathbb{E}\left[Y^{T=1}(t)\right]-\mathbb{E}\left[Y^{T=0}(t)\right] \\
\text { e.g. } & \text { (no confounder) } \\
\widehat{A C E}(t)= & \sum_{i=1}^{n_{1}} Y_{i}^{T=1}(t)-\sum_{j=1}^{n_{2}} Y_{j}^{T=0}(t)
\end{aligned}
$$

## G formula

Real world: confounders


## G formula

Real world: confounders
Statistical model: $\mathbb{E}[Y \mid X, T]$

$$
\begin{aligned}
\operatorname{ACE}(t)= & \sum_{i=1}^{n} \mathbb{E}\left[Y_{i}(t) \mid X_{i}, T=1\right] \\
& -\mathbb{E}\left[Y_{i}(t) \mid X_{i}, T=0\right]
\end{aligned}
$$

Here $Y(t) \mid X, T$ is the absolute risk

## Workflow (Christiansen et al. 2015)

(1) Define the population of interest

Patients with first-time ischemic stroke ( $n=19223$ )
Exclusion criteria: atrial fibrillation ...
(2) Define the intervention ( $T$ )
(3) Define the event of interest $(Y)$

## Workflow (Christiansen et al. 2015)

(1) Define the population of interest
(2) Define the intervention $(T)$
e.g.: antiplatelet regimens for secondary stroke prevention T=0: ASA
T=1: Clopidogrel
T=2: ASA+Clopidogrel
(3) Define the event of interest ( $Y$ )
(C) Identify the possible competing events $(D)$

## Workflow (Christiansen et al. 2015)

(1) Define the population of interest
(2) Define the intervention ( $T$ )
(3) Define the event of interest $(Y)$
e.g.: fatal or non fatal ischemic stroke
(4) Identify the possible competing events (D)
(3) Identify the possible confounders/pronostic variable $(X)$

## Workflow (Christiansen et al. 2015)

(1) Define the population of interest
(2) Define the intervention ( $T$ )
(3) Define the event of interest $(Y)$
(9) Identify the possible competing events $(D)$

```
e.g.: death not related to a stroke event
```(3) Identify the possible confounders/pronostic variable \((X)\) (6) Define a statistical model for relating

\section*{Workflow (Christiansen et al. 2015)}
(1) Define the population of interest
(2) Define the intervention ( \(T\) )
(3) Define the event of interest \((Y)\)
(9) Identify the possible competing events \((D)\)
(5) Identify the possible confounders/pronostic variable \((X)\) e.g. age, hypertension, ...

\section*{Workflow (Christiansen et al. 2015)}
(1) Define the population of interest
(2) Define the intervention \((T)\)
(3) Define the event of interest \((Y)\)
(4) Identify the possible competing events ( \(D\) )
(6) Identify the possible confounders/pronostic variable \((X)\)
(1) Define a statistical model for relating \(Y, T\), and \(X\)

A two-cause specific Cox model:
\[
\begin{aligned}
& \lambda^{Y}(t \mid X, T)=\lambda_{0}^{Y} e^{\beta^{Y} X+\gamma^{Y} T} \\
& \lambda^{D}(t \mid X, T)=\lambda_{0}^{D} e^{\beta^{D} X+\gamma^{D} T}
\end{aligned}
\]

\section*{Computation of the G-formula - in}

Package: riskRegression
https://github.com/tagteam/riskRegression Function: ate

Arguments
- object: outcome model which describes how event risk depends on treatment and covariates
- data
- treatment: name of the treatment variable in data
- times: time points at which to evaluate risks
- cause: the cause of interest
- B: the number of bootstrap replications used to compute the confidence interval.

\section*{G-formula (software)}

No competing risks:
> head (dtSurv)
\begin{tabular}{|c|c|c|c|c|}
\hline & time & nt & & Age \\
\hline 1 & 4.901849 & FALSE & & 59.78796 \\
\hline 2 & 4.555159 & TRUE & T0 & 60.66406 \\
\hline 3 & 6.681136 & FALSE & T1 & 58.76296 \\
\hline \multicolumn{5}{|l|}{```
> mCox <- coxph(Surv(time,strokeEvent)~ Treatment + Age,
+ data = dtSurv)
```} \\
\hline \multicolumn{5}{|l|}{```
    ate(mCox, data = dtSurv, treatment = "Treatment",
+ times = 12, B = 1000)
```} \\
\hline
\end{tabular}

\section*{G-formula (software)}

Competing risks:
> head(dtCR)
time eventtype eventtypeNum
1: Treatment Age

\section*{G-formula (software output)}

Absolute risk of stroke relapse
Treatment meanRisk meanRiskBoot lower upper n.boot
\begin{tabular}{lllllll}
\(1:\) & T0 & 0.111 & 0.111 & 0.101 & 0.123 & 1000 \\
\(2:\) & T1 & 0.080 & 0.080 & 0.071 & 0.090 & 1000 \\
\(3:\) & T2 & 0.078 & 0.078 & 0.073 & 0.082 & 1000
\end{tabular}

Difference in absolute risk of stroke between treatments:
\begin{tabular}{lrrrlr} 
Treatment.A & Treatment.B & time & diff & \\
1: & T1 & T0 & 12 & 0.032 & \\
2: & T2 & T0 & 12 & 0.034 & \\
3: & T2 & T1 & 12 & 0.002 & \\
& diffMeanBoot & diff. lower & diff. upper & n. boot \\
1: & 0.032 & 0.017 & \multicolumn{2}{c}{0.046} & 1000 \\
2: & 0.033 & 0.022 & 0.046 & 1000 \\
3: & 0.002 & 0.002 & 0.013 & 1000
\end{tabular}

\section*{Assumptions}
- no unmeasured confounders
- positivity
- well-defined intervention
-

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- no unmeasured confounders
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\(\triangleright\) proportional hazard assumption

\(\widehat{\text { ATE }}:-0.513[-0.571 ;-0.441]\) vs \(-0.244[-0.281 ;-0.206]\)

\section*{Assumptions}
- no unmeasured confounders
- positivity
- well-defined intervention
- correctly specified model
\(\triangleright\) proportional hazard assumption
\(\triangleright\) (linear) functional form
[Not covered] non-informative censoring,

\(\widehat{\text { ATE }}:-0.164[-0.221 ;-0.107]\) vs \(-0.200[-0.264 ;-0.132]\)

\section*{Assumptions}
- no unmeasured confounders
- positivity
- well-defined intervention
- correctly specified model
\(\triangleright\) proportional hazard assumption
\(\triangleright\) (linear) functional form
\(\triangleright\) (absence of) interaction

\(\widehat{\text { ATE }}:-0.110[-0.169 ;-0.049]\) vs \(-0.267[-0.302 ;-0.228]\)

\section*{Assumptions}
- no unmeasured confounders
- positivity
- well-defined intervention
- correctly specified model
\(\triangleright\) proportional hazard assumption
\(\triangleright\) (linear) functional form
\(\triangleright\) (absence of) interaction
[Not covered] non-informative censoring, influential observations

\section*{Proposed approach}
- Compare alternative modelling strategies to the Cox model \(\rightarrow\) check result sensitivity to model assumptions

Alternative models:
\(\checkmark\) increased flexibility:
\(\rightarrow\) less biased
\(X\) increased complexity:
\(\rightarrow\) harder to interpret
\(\rightarrow\) increased variance of the estimates

\section*{Extensions/alternatives to Cox model}
- relax PH assumption:
-Cox strata stratified Cox model
-Others Cox model with time varying effects logistic risk regression
- include non-linear relationships/interactions
-Cox spline regression spline in Cox model
-RF random survival Forest

\section*{Simulation study}

Investigate the bias/variance trade-off
Three scenari:
(I) violation of proportional hazard assumption
(II) mispecification of the functional form of a risk factor
(III) missing interaction with the treatment variable

\section*{Results - proportional hazard}
\begin{tabular}{llll}
\hline Scenario I & \multicolumn{3}{c}{ Non proportional effect of treatment } \\
\hline\(O R_{T}(t \leq 5)\) & 0.8 & 1.7 & 7.4 \\
\(O R_{T}(t \geq 5)\) & 0.4 & 0.4 & 0.4 \\
& & & \\
ATE & 0.181 & -0.002 & -0.068 \\
& & & \\
Cox & \(-0.049(0.05)\) & \(-0.082(0.083)\) & \(-0.062(0.062)\) \\
Cox strata & \(0.001(0.011)\) & \(0(0.01)\) & \(-0.01(0.013)\) \\
Random Forest & \(0.001(0.01)\) & \(0(0.009)\) & \(0.005(0.007)\)
\end{tabular}

Table: last three rows:
bias (root mean square error) of the ATE estimated by the models \(O R_{T}\) odd ratio for the treatment effect

\section*{Results - functional form}
\begin{tabular}{llll}
\hline Scenario II & \multicolumn{3}{c}{ Non linear effect of covariate } \\
\hline OR \(_{T}\) & 0.4 & 0.4 & 0.4 \\
OR Age & 0.8 & 2.7 & 7.4 \\
ATE & 0.338 & 0.338 & 0.338 \\
& & & \\
Cox & \(0.001(0.01)\) & \(0(0.01)\) & \(0(0.01)\) \\
Cox strata & \(0.001(0.011)\) & \(-0.001(0.011)\) & \(-0.001(0.011)\) \\
Random Forest & \(-0.003(0.011)\) & \(-0.004(0.012)\) & \(-0.004(0.012)\)
\end{tabular}

Table: last three rows:
bias (root mean square error) of the ATE estimated by the models \(O R_{T}\) odd ratio for the treatment effect \(O R_{\text {Age }}\) odd ratio for the non linear effect of the risk factor (increased risk after 50 years)

\section*{Results - interaction}
\begin{tabular}{llll}
\hline Scenario III & \multicolumn{3}{l}{ Interaction between treatment and covariate } \\
\hline\(O R_{T}\) & 0.4 & 0.4 & 0.4 \\
R \(_{T * \text { gender }}\) & 1.6 & 2.7 & 7.4 \\
ATE & & & \\
& 0.075 & -0.011 & -0.097 \\
Cox & \(-0.01(0.014)\) & \(-0.04(0.041)\) & \(-0.146(0.146)\) \\
Cox strata & \(0.001(0.011)\) & \(0(0.011)\) & \(0.001(0.01)\) \\
Random Forest & \(0.001(0.011)\) & \(0(0.011)\) & \(0(0.01)\)
\end{tabular}

Table: last three rows:
bias (root mean square error) of the ATE estimated by the models \(O R_{T}\) odd ratio for the treatment effect \(O R_{T * \text { gender }}\) odd ratio for interaction between gender and treatment

\section*{Discussion}

Alternative models:
\(\checkmark\) No noticeable increase of the variance of the estimates
\(\checkmark\) For categorical variables, a fully stratified Cox model is robust against:
- non PH
- interaction between variables
\(\checkmark\) For dealing with continuous variables, use random Forests
\(\mathbf{X}\) extra-parameters to be tuned (e.g. number of trees)
\(X\) Increased computation time

\section*{Application}

Objective:
- to compare 3 antiplatelet regimens using the danish registry
- \(\mathrm{n}=19223\) patients
- time horizon: 1 year

Outcome:
- date of first stroke event ( \(\mathrm{n}=1610,8.4 \%\) )

Competing event:
- death ( \(\mathrm{n}=677,3.5 \%\) )

Possible confounders:
- many ( \(p=10\) ) including age, gender, ...

\section*{Checking Proportional hazard assumption}


\footnotetext{
\({ }^{1}\) based on the score process
}

\section*{Checking functional form}

\section*{Variable age}
- additional risk after 75 years
- approx. linear


\section*{Models}

Variables:
- Continuous: age
- Categorical: treatment, gender, year

CSC CSC inter

Two cause specific Cox model CSC
+ interactions between treatment and gender, age, year
+ cubic spline on age
CSC strata stratified CSC on treatment, gender, year

\section*{naive Cox model vs. alternatives}

- violation of PH assumption impacts the estimate of NTT at early times

\section*{Summary}

Cox models can be used to assess :
\(\triangleright\) disease incidence (absolute risk)
\(\triangleright\) average treatment effect

Relies on several assumptions, e.g.:
\(\triangleright\) proportional hazard
\(\triangleright\) linear effect, no interaction between variables

Model checking:
\(\triangleright\) Hope: no unmeasured confounders
\(\triangleright\) usual diagnostic tools are of limited interest for large \(p\) or \(n\)
\(\triangleright\) proposal: assess the impact of Cox model assumptions using alternative models

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